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(1) $y' = \frac{a\sqrt{x^2-1} - 2x(ax+b)}{3\sqrt{(x^2-1)^3}} = \frac{3a(x^2-1) - 2ax^2 - 2xb}{3\sqrt{(x^2-1)^3}} = \frac{ax^2 - 2xb - 3ax}{3\sqrt{(x^2-1)^3}}$

$\Delta < 0$ $a \neq 0$ $a \neq 0$ $b \neq 0$ $4b^2 - 12a^2 < 0$
 $4b^2 - 12a^2 < 0$
 $12a^2 > 4b^2$ $3a^2 > b^2$ $a > \frac{b}{\sqrt{3}}$ $a < -\frac{b}{\sqrt{3}}$

(2) (1) $x^2 - 1 \neq 0$
 $\frac{x}{x^2-1}, x \neq \pm 1$

(2) $\lim_{x \rightarrow 1^+} \frac{x}{x^2-1} = \frac{1}{+0} = \infty \rightarrow [x=1]$

$\lim_{x \rightarrow -1^-} \frac{x}{x^2-1} = \frac{-1}{-0} = \infty \rightarrow [x=-1]$

$m = \lim_{x \rightarrow \infty} \frac{x}{x\sqrt{x^2-1}} = 0$ $n = \lim_{x \rightarrow -\infty} \frac{x}{x\sqrt{x^2-1}} = 0$

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(3) $y(0) = 0$

$0 = \frac{x}{\sqrt{x^2-1}} \rightarrow x=0 \rightarrow (0,0)$

(4) $y' = \frac{x^2-3}{3\sqrt{(x^2-1)^3}} \rightarrow x = \pm\sqrt{3}$

$x > \sqrt{3}, x < -\sqrt{3}$: \nearrow \nearrow
 $-1 < x < 1, -\sqrt{3} < x < -1, 1 < x < \sqrt{3}$: \searrow \searrow
 $\max(-\sqrt{3}, \frac{\sqrt{3}}{2})$ $\min(\sqrt{3}, \frac{\sqrt{3}}{2})$

-2	$-\sqrt{3}$	$-\frac{1}{2}$	-1	0	1	$\frac{1}{2}$	$\sqrt{3}$	2
+	0	-	-	0	+	+	0	+
\nearrow	max	\searrow	\searrow	0	\nearrow	\nearrow	min	\nearrow

(5) $y'' = \frac{2x \cdot 3\sqrt{(x^2-1)^4} - 3 \cdot \frac{2}{3}(x^2-1)^{\frac{1}{3}}(x^2-3) \cdot 2x}{9^3 \sqrt{(x^2-1)^{12}}} = \frac{6x(x^2-1)^{\frac{1}{3}} - 4(x^2-3) \cdot 2x}{9^3 \sqrt{(x^2-1)^{12}}}$

$6x^3 - 6x - 8x^3 + 24x = 0$
 $-2x^3 + 18x = 0$
 $-2x(x^2 - 9) = 0$
 $x = 0, x = \pm 3$

(3, $\frac{3}{\sqrt{8}}$) $\sqrt{10}$ π

-1	-2	-1	0	1	2	3	4
+	+	-	0	-	+	+	-

