



1.73
5 10 $\triangle A O_1 C \sim \triangle D O_2 C$ (S.S)

$$\frac{O_1 A}{O_2 D} = \frac{O_1 C}{O_2 C}$$

$$\frac{R}{r} = \frac{R+2r+kC}{r+kC}$$

$$Rr + RkC = Rr + 2r^2 + r \cdot kC$$

$$kC = \frac{2r^2}{R-r}$$

$$\sin \alpha = \frac{D O_2}{O_2 C} = \frac{r}{r + \frac{2r^2}{R-r}} = \frac{(R-r)r}{Rr+r^2} =$$

$$= \frac{(R-r)r}{(R+r)r} = \frac{R-r}{R+r}$$

\therefore

$$\alpha = \angle O_2 D E$$

$$\sin \alpha = \frac{O_2 M}{O_2 D} = \frac{R-r}{R+r} = \frac{\frac{R}{2} - \frac{r}{2}}{\frac{R}{2} + \frac{r}{2}} = \frac{1 - \frac{a}{b}}{1 + \frac{a}{b}} = \frac{b-a}{b+a}$$

(S.S) $\triangle O_1 A N \sim \triangle O_2 D M$

$$\frac{r}{R} = \frac{\frac{1}{2}a}{\frac{1}{2}b}$$

$$\frac{r}{R} = \frac{a}{b}$$