

1.117  
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$$(2^x - 2 \cdot 2^{-x}) \log_9(2x+3) - \log_3 x = 1$$

$$\begin{aligned} 2^x \cdot 2 \cdot 2^{-x} &= 1 \\ 2^x \cdot 2 &= \frac{2}{2^x} = 1 \\ 2^x &= t \\ t - \frac{2}{t} &= 1 \\ t^2 - t - 2 &= 0 \\ t = 2 \quad t = -1 \\ \frac{2^x = 2}{x=1} \quad \frac{2^x = -1}{\emptyset} \end{aligned}$$

$$\begin{aligned} \rightarrow \log_9(2x+3) - \log_3 x &= 0 \\ \frac{1}{2} \log_3(2x+3) &= \log_3 x \\ \log_3 \sqrt{2x+3} &= \log_3 x \\ \sqrt{2x+3} &= x \\ 2x+3 &= x^2 \\ x^2 - 2x - 3 &= 0 \\ \boxed{x=5} \quad \boxed{x=-1} \end{aligned}$$

$$\boxed{x > 0} \left\{ \begin{array}{l} x > 0 \\ x > -\frac{1}{2} \leftarrow 2x+3 > 0 \end{array} \right.$$

אחר כך מנמיכים את הפונקציה

$$\boxed{x=1,3} \quad ; \text{ההגדרה}$$