

1.55  
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$$\log_x 2 \cdot \log_{2x} 2 \cdot \log_2 4x > 1$$

$$\log_x 2 \cdot \log_{2x} 2 \cdot (\log_2 4 + \log_2 x) > 1$$

$$\log_x 2 \cdot \frac{1}{\log_2 2x} \cdot (2 + \log_2 x) > 1$$

$$\log_x 2 \cdot \frac{1}{\log_2 2 + \log_2 x} \cdot (2 + \log_2 x) > 1$$

$$\frac{1}{t} \cdot \frac{1}{1+t} \cdot (2+t) > 1$$

$$\log_2 x = t \quad (10)$$

$$0 < \frac{2+t-t-t^2}{t(1+t)} = \frac{2-t^2}{t(1+t)}$$

$$\begin{array}{ccccccc} & & & + & & & \\ & & & -\sqrt{2} & -1 & -0 & \sqrt{2} \\ & & & & & & - \end{array}$$

$$0 < t < \sqrt{2} \rightarrow 0 < \log_2 x < \sqrt{2} \rightarrow 1 < x < 2^{\sqrt{2}}$$

$$-\sqrt{2} < t < -1 \rightarrow -\sqrt{2} < \log_2 x < -1 \rightarrow 2^{-\sqrt{2}} < x < \frac{1}{2}$$