

1.77 ① $[\log_{x+6} 2] \log_2 (x^2 - x - 2) \geq 1$

$\frac{\log_2 2}{\log_2 (x+6)} \cdot \frac{\log_2 [(x-2)(x+1)]}{\log_2} \geq 1$

$0 < x+6 < 1 \Rightarrow -6 < x < -3$
 $(x-2)(x+1) \leq x+6$
 $x^2 - 2x - 8 \leq 0$
 $-2 \leq x \leq 4$

$\log_{x+6} [(x-2)(x+1)] \geq 1$
 $(x-2)(x+1) \geq x+6$
 $x^2 - 2x - 8 \geq 0$
 $x \geq 4$ or $x \leq -2$

$-5 < x < -6 \leftarrow 1 \neq x+6 > 0$
 $\frac{1}{-1} \frac{1}{2} \leftarrow x^2 - x - 2 > 0$

$-5 < x < -1$
 $-6 < x < -5$
 $x > 2$

$x \geq 4$
 $-5 < x \leq -2$
~~transparens~~

② $y = \log_3 (0.64^{2 - \log_{\sqrt{2}} x} - 1.25^{8 - \log_2^2 x})$

$0.64^{2 - \log_{\sqrt{2}} x} - 1.25^{8 - \log_2^2 x} > 0$

$x > 0$

$(\frac{16}{25})^{2 - \log_{\sqrt{2}} x} > (\frac{5}{4})^{8 - \log_2^2 x}$

$(\frac{4}{5})^{4 - 2 \log_{\sqrt{2}} x} > (\frac{4}{5})^{\log_2^2 x - 8}$

$4 - 2 \log_{\sqrt{2}} x < \log_2^2 x - 8$

$4 - \frac{2}{0.5} \log_2 x < \log_2^2 x - 8$

$4 - 4 \log_2 x < \log_2^2 x - 8$

$\log_2 x = t$ / no/

$0 < t^2 + 4t - 12$

$t < -6$ or $t > 2$

$\log_2 x < -6 \rightarrow x < 2^{-6}$

$x < \frac{1}{64}$

$\log_2 x > 2$

$x > 4$