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$$a_1 = \sqrt{2} \quad 2S_n = S \rightarrow \frac{2a_1(q^n - 1)}{q - 1} = \frac{a_1}{1 - q} \rightarrow -2(q^{n-1}) = 1 \rightarrow [q^n = -\frac{1}{2} + 1 = \frac{1}{2}]$$

$$\prod_{i=1}^n a_i = a_1 \cdot a_2 \cdot \dots \cdot a_n = a_1 \cdot (a_1 q) \cdot (a_1 q^2) \cdot \dots \cdot (a_1 q^{n-1}) = a_1^n q^{1+2+\dots+n-1} = a_1^n q^{\frac{n-1}{2} \cdot n} = a_1^n q^{\frac{n^2-n}{2}}$$

$$= [a_1^n q^{\frac{n-1}{2}}]^n = \sqrt{2}^n q^{\frac{n^2}{2}} \cdot q^{-\frac{n}{2}} = (\sqrt{2})^n (q^n)^{\frac{n}{2}} \cdot (q^n)^{-\frac{1}{2}} = (\sqrt{2})^n \cdot \left(\frac{1}{2}\right)^{\frac{n}{2}} \cdot \left(\frac{1}{2}\right)^{-\frac{1}{2}} =$$

$$= (\sqrt{2})^n \cdot \left(\frac{1}{2}\right)^{\frac{n}{2}} \cdot 2^{\frac{1}{2}} \cdot 2^{-\frac{n}{2}} \cdot \sqrt{2} = \sqrt{2}$$