

2.10
5

$$1 + \tan^2 \alpha = \frac{1}{\cos^2 \alpha}$$

$$1 + \frac{a^2}{b^2} = \frac{1}{\cos^2 \alpha}$$

$$\frac{b^2 + a^2}{b^2} = \frac{1}{\cos^2 \alpha}$$

$$\cos^2 \alpha = \frac{b^2}{a^2 + b^2}$$

find α when $\tan \alpha = \frac{a}{b}$
if $\sin \alpha = \frac{a}{\sqrt{a^2 + b^2}}$ then $\cos \alpha = \frac{b}{\sqrt{a^2 + b^2}}$

$$\tan \alpha = \frac{\sin \alpha}{\cos \alpha}$$

$$\sin \alpha = \tan \alpha \cdot \cos \alpha = \frac{a}{b} \cdot \left(\frac{b}{\sqrt{a^2 + b^2}} \right) = \frac{a}{\sqrt{a^2 + b^2}}$$

$$\cos \alpha = \frac{1}{\tan \alpha} = \frac{b}{a}$$