

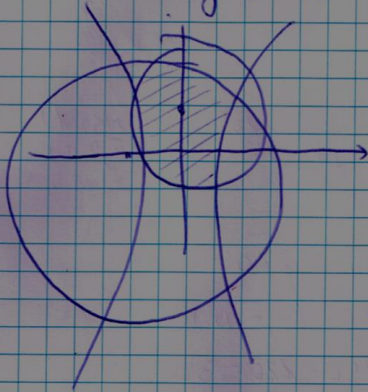
3,50  
8

(i)  $4 \geq |z+1| = \sqrt{(x+1)^2 + y^2} \rightarrow (x+1)^2 + y^2 \leq 16 \rightarrow$  radius 2

$1 > \operatorname{Re}(z^2) = \operatorname{Re}(x^2 + 2xyi - y^2) \rightarrow x^2 - y^2 < 1 \rightarrow$  hyperbola

$5 > |z|^2 - 2\operatorname{Im}(2z) = x^2 + y^2 - 4y = x^2 + (y-2)^2 - 4$

$x^2 + (y-2)^2 < 9 \rightarrow$  radius 3



$q = \frac{2i}{1+i} \cdot \frac{1-i}{1-i} = \frac{2i+2}{2}$  (ii)

$q = 1+i$

$S_{12} = \frac{(1+i)[(1+i)^2 - 1]}{1+i-1} = \frac{(1+i)^2 - 1}{i}$

$(1+i) = \sqrt{2} \operatorname{cis} 45$

$(1+i)^2 = (\sqrt{2} \operatorname{cis} 45)^2 = 2 \operatorname{cis} 90 = 2i$

$S_{12} = \frac{(1+i)(2i-1)}{i} = \frac{-65(1+i)(i)}{1} = -65 + 65i$

(E)  $\left| \frac{(3+4i)(1+i)^6}{i^5(2+4i)} \right| = \frac{|3+4i| |1+i|^6}{|i|^5 |2+4i|} = \frac{5 \cdot (\sqrt{2})^6}{1^5 \sqrt{20}} = \frac{5 \cdot 8}{\sqrt{20}}$

$= \frac{40}{2\sqrt{5}} = \frac{20}{\sqrt{5}} = \frac{20\sqrt{5}}{5} = 4\sqrt{5}$