

3.68
2

(*)

$$z^4 = -2 + i\sqrt{12} = 4 \operatorname{cis} 120$$

$$r = \sqrt{4+12} = 4$$

$$\tan \theta = \frac{\sqrt{12}}{-2} = -\sqrt{3} \rightarrow \theta = 120$$

$$z_k = \sqrt[4]{4} \operatorname{cis}(30 + 90k) = \sqrt{2} \operatorname{cis}(30 + 90k) \quad k=0,1,2,3$$

(*)

$$|z| \geq |z|^2 + 2 \operatorname{Im} z = x^2 + y^2 + 2y \rightarrow x^2 + (y+1)^2 \leq 16$$

$$|z-2i| \leq |z| \rightarrow (x)^2 + (y-2)^2 \leq x^2 + y^2 \rightarrow y \geq 1$$

