

3.73
18

$$i) \quad \eta = \frac{i-1}{1+i} = \frac{\sqrt{2} \operatorname{cis} 135}{\sqrt{2} \operatorname{cis} 45} = \operatorname{cis} 90 = i$$

$$S_{10} = \frac{(1+i)(i^{10}-1)}{i-1} = \frac{(1+i)(-2)}{i-1} = \frac{-2}{i} = \frac{-2 \cdot (-i)}{1} = 2i$$

$$ii) \quad \left| \frac{(1+i)^8 (2i-4)^2}{5i \left(\sin \frac{3\pi}{4} + i \cos \frac{\pi}{4} \right)} \right| = \left| \frac{(\sqrt{2} \operatorname{cis} 45)^8 (5 \operatorname{cis}(\arctan(-\frac{3}{4})))^2}{5i \left(\cos(\frac{\pi}{4}) + i \sin(\frac{\pi}{4}) \right)} \right| =$$

$$\left| \frac{16 \operatorname{cis} 360 \cdot 25 \operatorname{cis}(\arctan(-\frac{3}{4}))}{5i \operatorname{cis}(\frac{\pi}{4})} \right| = \frac{|16 \operatorname{cis} 360| \cdot |25 \operatorname{cis}(\arctan(-\frac{3}{4}))|}{|5i| \cdot |\operatorname{cis} \frac{\pi}{4}|} =$$

$$= \frac{16 \cdot 25}{5 \cdot 1} = 80$$

3.73
19

$$z^4 = -\frac{3}{2} - \frac{\sqrt{3}}{2}i = \sqrt{3} \operatorname{cis} \left(\frac{7\pi}{6} \right)$$

$$r = \sqrt{\frac{9}{4} + \frac{3}{4}} = \sqrt{3}$$

$$\tan \theta = \frac{-\frac{\sqrt{3}}{2}}{-\frac{3}{2}} = \frac{1}{\sqrt{3}} \rightarrow \theta = 210$$

$$z_k = \sqrt[4]{3} \operatorname{cis} \left(\frac{7\pi}{24} + \frac{\pi k}{2} \right) \quad k=0, 1, 2, 3$$