

4.7  
3

$$\left(\frac{2}{3}\right) \log_{0.5}(x^2+4x+4) < \left(\frac{9}{4}\right) \log_2(x^2-3x-10)$$

$$\left(\frac{2}{3}\right) \log_{2^{-1}}(x^2+4x+4) < \left(\frac{9}{4}\right) 2 \log_2(x^2-3x-10)$$

$$\left(\frac{2}{3}\right) - \log_2(x^2+4x+4) < \left(\frac{9}{2}\right) 2 \log_2(x^2-3x-10)$$

$$\left(\frac{2}{3}\right) \log_2(x+2)^2 < \left(\frac{9}{2}\right) 2 \log_2(x^2-3x-10)$$

$$\log_2(x+2)^2 < \log_2(x^2-3x-10)^2$$

$$(x+2)^2 < (x-5)^2(x+2)^2$$

$$0 < (x+2)^2((x-5)^2-1)$$

$$\downarrow \quad \downarrow$$
$$x = -2 \quad x^2 - 10x + 24 = 0$$

$$x \geq 6 \quad x \leq 4$$

! n n f n p h n

$$x^2 - 3x - 10 > 0 \quad \text{! n n f n} \quad x^2 + 4x + 4 > 0$$

$$(x-5)(x+2) > 0 \quad \text{! n} \quad (x+2)^2 > 0$$

$$\boxed{x < -2 \quad x > 5}$$

$$\boxed{x \neq -2}$$

$$\boxed{x < -2 \quad x > 5}$$

! p h o f

$$\begin{array}{c} + \quad + \quad + \\ * - 2 \quad 4 \quad - 6 \end{array}$$

$$\boxed{x < -2 \quad 2 < x < 4 \quad x > 6}$$

$$\boxed{x < -2 \quad x > 6}$$

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