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$$\begin{aligned}
 3 - \sin 4x + 3 \sin 2x - 3 \cos 2x &= 0 \\
 3 - 2 \sin 2x \cos 2x + 3 \sin 2x - 3 \cos 2x &= 0 \\
 2 + \underbrace{1 - 2 \sin 2x \cos 2x}_{t^2} + 3(\sin 2x - \cos 2x) &= 0 \\
 2 + (\sin 2x - \cos 2x)^2 + 3(\sin 2x - \cos 2x) &= 0 \\
 t^2 + 3t + 2 &= 0
 \end{aligned}$$

$$t = -2$$

$$\sin 2x - \cos 2x = -2$$

$$\begin{aligned}
 \frac{\sqrt{2}}{\sqrt{2}} \left( \frac{\sqrt{2}}{2} \sin 2x - \frac{\sqrt{2}}{2} \cos 2x \right) &= -2 \\
 \cos 45^\circ \sin 2x - \sin 45^\circ \cos 2x &= -\sqrt{2} \\
 \sin \left( 2x - \frac{\pi}{4} \right) &= -\sqrt{2} \\
 \emptyset
 \end{aligned}$$

$$\sin 2x - \cos 2x = -1$$

$$\frac{1}{\sqrt{2}} \sin \left( 2x - \frac{\pi}{4} \right) = -1$$

$$\sin \left( 2x - \frac{\pi}{4} \right) = -\frac{\sqrt{2}}{2} = \sin \left( -\frac{\pi}{4} \right)$$

$$2x - \frac{\pi}{4} = -\frac{\pi}{4} + 2\pi k \quad \left| \quad 2x - \frac{\pi}{4} = \frac{5\pi}{4} + 2\pi k \right.$$

$$\boxed{x = \pi k}$$

$$\boxed{x = \frac{3\pi}{4} + \pi k}$$

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$$\begin{aligned}
 \cos^2 x + \cos^2(x+\alpha) - 2 \cos x \cos \alpha \cdot \cos(x+\alpha) &= \\
 \cos^2 x + \cos(x+\alpha) [\cos(x+\alpha) - 2 \cos x \cos \alpha] &= \\
 \cos^2 x + \cos(x+\alpha) [\cos(x+\alpha) - \cos(x-\alpha) - \cos(x-\alpha)] &= \\
 \cos^2 x + \cos(x+\alpha) \cos(x-\alpha) &= \\
 \cos^2 x + \frac{1}{2} \cos(2x) + \frac{1}{2} \cos 2\alpha &= \\
 \cos^2 x + \frac{1}{2} (2 \cos^2 x - 1) + \frac{1}{2} \cos 2\alpha &= \frac{1}{2} (\cos 2\alpha + 1)
 \end{aligned}$$