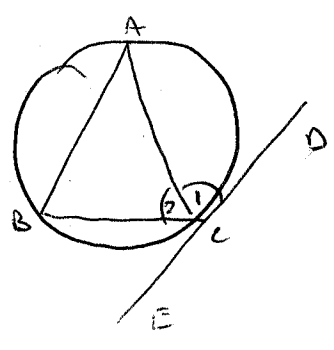


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$\angle C_1 = \beta$ (given)

(inscribed angles subtending the same arc) $\angle B = \angle C_1 = \beta$
 (same arc AB subtended by the same angle)

\Downarrow
 (given) $\angle B = \angle C_2$
 \Downarrow
 $\angle C_1 = \angle C_2$

$\angle B = \frac{180 - \angle A}{2} = \frac{180 - \alpha}{2} = 90 - \frac{\alpha}{2}$

(inscribed) $\angle ACD = \angle B = 90 - \frac{\alpha}{2}$

$180 = \angle C = \angle C_1 + \angle C_2 + \angle BCE$ (given) $\angle B = \angle C_1 = \angle C_2$

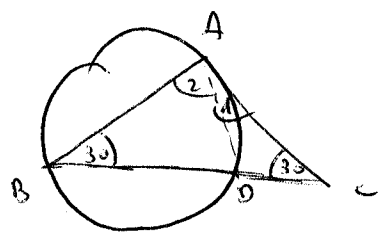
$180 = \angle B + \angle B + \angle BCE$

$180 = 90 - \frac{\alpha}{2} + 90 - \frac{\alpha}{2} + \angle BCE$

$180 = 180 - \alpha + \angle BCE$

$\angle BCE = \alpha$

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(given) $\angle A = 120$

(triangle ABC \rightarrow inscribed) $\angle A = 120$

(inscribed angles subtending the same arc) $\angle A_1 = \angle B = 30$
 (same arc AC subtended by the same angle)

\Downarrow
 $\angle A_2 = \angle A - \angle A_1 = 90$

BD is a diameter

$\angle A_1 = \angle C = 30$

\Downarrow
 $AD = DC$

Triangle ABD is a 30-60-90 triangle. The hypotenuse is BD. The side opposite 30 is AD. $AD = \frac{1}{2} BD = r$

(DC) $AD = \frac{1}{2} BD = r$

$BC = BD + DC = 2r + r = 3r$